

DATA SET CATALOG #159

PROGRAM MAGTAL

RA7712

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## **1. INTRODUCTION:**

The documentation for this data set was originally on paper, kept in NSSDC's Data Set Catalogs (DSCs). The paper documentation in the Data Set Catalogs have been made into digital images, and then collected into a single PDF file for each Data Set Catalog. The inventory information in these DSCs is current as of July 1, 2004. This inventory information is now no longer maintained in the DSCs, but is now managed in the inventory part of the NSSDC information system. The information existing in the DSCs is now not needed for locating the data files, but we did not remove that inventory information.

The offline tape datasets have now been migrated from the original magnetic tape to Archival Information Packages (AIP's).

A prior restoration may have been done on data sets, if a requestor of this data set has questions; they should send an inquiry to the request office to see if additional information exists.

## 2. ERRATA/CHANGE LOG:

NOTE: Changes are made in a text box, and will show up that way when displayed on screen with a PDF reader.

*When printing, special settings may be required to make the text box appear on the printed output.*

Version	Date	Person	Page	Description of Change
01				
02				

3 LINKS TO RELEVANT INFORMATION IN THE ONLINE NSSDC INFORMATION SYSTEM:

<http://nssdc.gsfc.nasa.gov/nmc/>

[NOTE: This link will take you to the main page of the NSSDC Master Catalog. There you will be able to perform searches to find additional information]

4. CATALOG MATERIALS:

- a. Associated Documents      To find associated documents you will need to know the document ID number and then click here.  
<http://nssdcftp.gsfc.nasa.gov/miscellaneous/documents/>

- b. Core Catalog Materials

## Nightside Magnetosphere Configuration as Obtained from Trapped Electrons at 1100 Kilometers

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**Abstract.** Using data from the polar orbiting satellite 1963-38C, we have obtained the diurnal variation of trapped electrons of energies  $E \geq 280$  kev and  $\geq 1.2$  Mev during magnetic quiet. This diurnal variation is measured as a latitude shift for constant electron intensity and is obtained as a function of invariant magnetic latitude. All the data were obtained for dipole orientations within  $\pm 12^\circ$  from the normal to the earth-sun line and for satellite positions within  $8^\circ$  of the noon-midnight meridian. Assuming conservation of the adiabatic invariants as these trapped electrons drift in the magnetosphere, it has been possible to obtain a nightside magnetic field configuration that fits the observed diurnal variations. A dayside configuration that agrees with experimental observations was used. The nightside configuration so determined displays an extended field line geometry and a current sheet in the magnetic equatorial plane. The field due to this current sheet is found to range from 20 to 40 gammas adjacent to the sheet, depending upon the radial extent of the sheet. A field line configuration in the noon-midnight meridian is presented. The nightside trapping boundary as defined by field line closure was found to occur at 1100 km at  $67^\circ$ , in agreement with observed boundaries at 1100 km of  $\sim 67^\circ$  for both  $\geq 40$ - and  $\geq 280$ -kev electrons. The situation on the dayside is different and is discussed.

### INTRODUCTION

Observations of a diurnal variation in the trapped electron population at high latitudes have been reported by *O'Brien* [1960], *McDiarmid and Barrois* [1964a and b], and *Frank et al.* [1964]. All these observations were concerned with electrons of energies  $\geq 40$  kev, and they showed that the observed diurnal latitudinal shifts at high latitude and low altitude were greater than could be explained by the conservation of the  $L$  invariant in a distorted magnetic field represented by the use of an image dipole [Mabille, 1960]. *Frank et al.* [1964] found that, to obtain the large diurnal shifts, it was necessary to add to the dipole field a field normal to the equator but oppositely directed on the dayside and nightside hemispheres, an assumption physically hard to justify.

Measurements of the diurnal shift of  $\geq 280$ -kev trapped electrons [Williams and Palmer, 1965] showed that these higher-energy electrons display a significantly smaller diurnal latitude shift during periods of magnetic quiet than the

$\geq 40$ -kev electrons do. An initial qualitative analysis by Williams and Palmer [1965] suggested that the diurnal shift of  $\geq 280$ -kev trapped electrons might possibly be explained by invariant conservation in a distorted magnetosphere such as described by Mead [1964].

The present, more detailed, quantitative study obtains the latitudinal dependence of the diurnal shift of  $\geq 280$ -kev and  $\geq 1.2$ -Mev electrons by determining latitudes of equal flux on the noon and midnight meridians. We find that the addition of a current sheet in the tail of Mead's model, leading to an 'open' field line configuration in the nightside hemisphere, is needed to fit the observed latitude shifts. By an 'open' configuration we simply mean one in which northern and southern high-latitude field lines do not connect, i.e., conjugate-point phenomena are not observed. This nightside field configuration is quite similar to configurations recently suggested by *Dessler and Juday* [1965] and *Axford et al.* [1965], and recently measured by the magnetometer on trap 1 [Voss, 1965].

We thus find that the observed diurnal variations of high-energy ( $E \geq 280$  kev) trapped

electrons are consistent with the drift of these particles in a distorted magnetosphere under the conservation of the adiabatic invariants  $\mu$  and  $J$ , and the conservation of energy  $E$ .

The experimental observations, the magnetospheric distortions, and the experimental and theoretical comparisons are described in subsequent sections.

#### EXPERIMENTAL RESULTS

*Satellite and experiment.* A more detailed description of the satellite and the detector may be found in *Williams and Smith* [1965].

Briefly, the data were obtained from the satellite 1965-38C, launched on September 28, 1963, into a nearly circular polar orbit having a 1140-km apogee, 1067-km perigee, 89.9° inclination, and 107.5-minute period. The satellite was magnetically aligned and displayed an oscillation of  $< \sim 6^\circ$  about the local line of force some 3 days after launch. Just after launch the satellite orbital plane made an angle of  $\sim 6^\circ$  with the noon-midnight meridian and was moving toward the noon-midnight meridian at the approximate rate of  $1^\circ$  per day owing to the earth's motion about the sun.

The detectors of interest comprise an integral electron spectrometer sensitive to electrons in the following energy ranges:  $E \geq 280$  kev,  $\geq 1.2$  Mev,  $\geq 2.4$  Mev, and  $\geq 3.6$  Mev. The spectrometer detecting channels of interest have full viewing angles of  $12^\circ$  and are oriented to look out normal to the satellite alignment axis. This is well removed from the loss cone at 1100 km, and the spectrometer therefore observes trapped electrons mirroring at the point of observation.

The spectrometer is essentially insensitive to protons of energy  $\lesssim 180$  Mev. The monitoring of an onboard proton spectrometer has shown that proton contamination is negligible for the data presented here.

*Pertinent information.* In trying to arrive at an ambient configuration for the magnetospheric cavity that is consistent with the experimental observations, we have used only data from magnetically quiet periods and have not considered any details of the observed correlation of increases in radiation cavity distortions with increases in magnetospheric distortions as obtained during magnetically active periods [*Williams and Palmer, 1965*].

The data are obtained from October 2 through October 12, 1963, which is the magnetically quiet period used by *Williams and Palmer* [1965] as their period 1. During this time the satellite orbital plane was within  $8^\circ$  of the noon-midnight meridian. Some 47 dayside passes and 28 nightside passes, obtained from the Navy receiving stations at College, Alaska, and Winkfield, England, have been analyzed. Few, if any, nightside data are available from the remaining stations in our station network.

The data are analyzed in terms of the invariant latitude,  $\Lambda$ , defined at satellite altitude as

$$\cos \Lambda = \sqrt{1.17/L}$$

where  $L$  is as defined by *Mellwin* [1961] and is obtained from a 4S coefficient expansion of the earth's magnetic field. Therefore, although still useful as a measure of magnetic latitude in low-altitude orbits,  $L$ , as here calculated, loses its significance at altitudes of  $\geq 4$  earth radii, where distortions due to the incident solar wind are generally considered to become noticeable. When a more accurate representation of the earth's magnetic field is used in obtaining the parameter  $L$ , it becomes apparent that  $L$  is no longer constant along a real line of force that reaches out to  $\geq 4$  earth radii, and this offers no conceptual advantage over the second invariant,

$$J = \oint p_\parallel ds$$

in these more distant regions.

To avoid confusion, we note here that the values of  $\Lambda$  quoted in *Williams and Palmer* [1965] were obtained from the surface values,  $\cos \Lambda = 1/\sqrt{L}$ . Those values should be corrected to satellite altitude, as there is a small but noticeable effect ( $\sim 1.5^\circ$ ) in the quoted latitude at which a given latitude shift is observed.

The particles being studied are trapped electrons of energies  $E_e \geq 280$  kev and  $E_e \geq 1.2$  Mev, having very small equatorial pitch angles. Absolute flux values, accurate to  $\sim 5.0\%$  in the 280-kev and 1.2-Mev channels, may be obtained by multiplying the observed count rates, respectively, by  $5(10)^2$  (cm<sup>2</sup> sec ster)<sup>-1</sup> and  $10^3$  (cm<sup>2</sup> sec ster)<sup>-1</sup>.

Any dependence of electron intensities on  $B$  value is dwarfed by the observed diurnal shift. The  $B$  dependence may be assumed to be relatively small since, at low altitude and high

$B$  values, a given fractional change in the mirror point  $B$  value being observed produces but a very small change in the equatorial pitch angle being sampled [Williams and Kohl, 1965].

*Data and data analysis.* All the data in the interval October 2 through October 12, 1963, were plotted on a scatter plot of count rate versus invariant latitude for both the dayside and nightside hemispheres. Composite curves, representative of the average count rates in this time interval, were then constructed from the scatter plots. This process is described and examples are shown in Williams and Palmer [1965].

We show in Figure 1 the day and night composite curves for this time interval as obtained by Williams and Palmer [1965] but now displayed as a function of latitude. We now include the composite curves for electrons of energy  $E_0 \geq 1.2$  Mev and see that the higher-energy electrons behave like the 280-kev electrons.

Looking at Figure 1 we see that the separation of the day and night curves can be explained either (a) by a vertical shift, i.e., an intensity change in the trapped electron population which is dependent on latitude, or (b) by a horizontal (latitude) shift, which is also dependent on latitude, or by both. It turns out that (a) requires the establishment of permanent injection mechanisms and/or permanent acceleration mechanisms capable of moving the mirror points of these trapped electrons great distances up and down lines of force. Correspondingly, (b) can be accomplished by a shift in latitude of the trapped electron population being observed and might be explained simply by the azimuthal drift of the electrons in a distorted magnetosphere under the conservation of the adiabatic invariants. It is this possible explanation of the observed diurnal shift that we are investigating in this report.

Extending the results of Masch [1961], we find that acceleration effects due to electric fields associated with geomagnetic variations yield energy gains of  $\approx 10^4$  e.v. at 280 kev. Thus, though important at low energies ( $\sim 1$  kev), these electric fields are apparently unimportant in determining trapped electron behavior at high energies ( $\geq 280$  kev). Furthermore, Masch shows that such electric fields accelerate electrons so that peak energies are reached at local midnight. This is opposite to

the diurnal variation observed by integral threshold detectors where trapped electron intensities are higher at noon than at midnight.

The curves shown in Figure 1 are a good representation of the diurnal shift phenomenon at low altitudes and high latitudes. Although useful results can be obtained from these curves, we believe that more accurate ones can be obtained by using (1) data from 'matched' passes only and (2) data obtained from daily averages of dayside and nightside count rate versus  $\Lambda$  plots. The main reason for our belief is that the curves of Figure 1 are affected by (a) slight changes in magnetic activity occurring throughout the time period and (b) an uneven distribution of the relative proportion of day and night passes throughout the time interval. The uneven distribution when coupled with the observed steady decay in intensity observed throughout the period under study [Williams and Smith, 1965; Williams and Palmer, 1965]

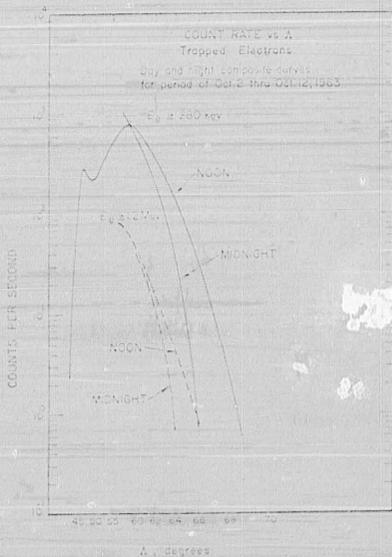


Fig. 1. Day and night count rate versus  $\Lambda$  composite curves for the magnetically quiet period October 2-12, 1963. Curves are shown for both  $E_0 \geq 280$  kev and  $\geq 1.2$  Mev. No night data are available for  $\Lambda \geq 55^\circ$ .  $\Lambda$  is defined at satellite altitude:  $\cos \Lambda = \sqrt{1.17/L}$ .

could yield errors in the diurnal shifts as obtained from the composite curves of Figure 1. We find that such errors are indeed small but are noticeable when comparisons are made with predictions of various magnetospheric models. We shall now discuss the data analyses (1) and (2) mentioned above.

1. Matched pass data. It is these data that yield the most accurate results for the values of the diurnal shifts at various latitudes. The matched passes are satellite passes observed by College, Alaska, and Winkfield, England, which, when used in conjunction with each other, trace the satellite from nightside, through the polar region, and on into the dayside hemisphere, or vice versa. Such pairs of passes, being but minutes apart and on reciprocal longitudes, eliminate a great amount of the scatter due to magnetic activity. These matched passes are as close as we are able to come to the ideal of simultaneous observation of the day and nightside latitude profile.

Of the 13 sets of matched passes obtained, College, Alaska, recorded 10 nightside and 3 dayside passes while Winkfield, England, conversely recorded 3 nightside and 10 dayside passes.

Now, assuming that the shifts shown in Figure 1 are due to a shift in latitude of the electron population as it drifts from the dayside to the nightside hemisphere, we have obtained from each of the matched pass pairs, the latitudes where the same count rates were observed on both the noon and midnight meridians. This was done for both the  $\geq 280$ -kev and  $\geq 1.2$ -Mev channels; the results of all the matched pass sets are shown in Figure 2 where we have plotted the nighttime latitude  $\Delta_N$  versus the daytime latitude  $\Delta_D$  observed for the condition of constant count rate.

Note that, in spite of a certain amount of scatter in the points of Figure 2, there does exist a well-defined latitude dependence of the diurnal variation for high-energy electrons. Also

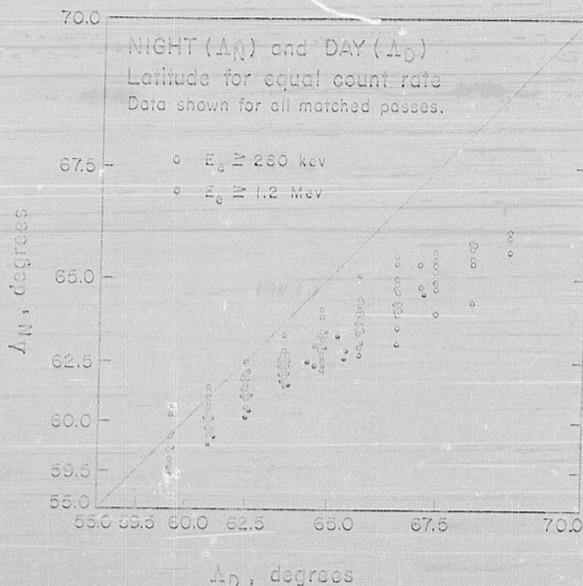


Fig. 2. Plot of  $\Delta_N$  versus  $\Delta_D$  for condition of constant count rate. All matched pass data are shown, both for  $E_0 \geq 280$  kev and  $E_0 \geq 1.2$  Mev. For the case of no solar wind in pure dipole field, the data would lie on the  $\Delta_N = \Delta_D$  line.

TABLE 1. Electron Intensities ( $E_e \geq 280$  kev) at  $\lambda = 65.8^\circ$  on Noon-Midnight Meridian throughout October 3, 1963

Noon			Midnight		
Time, UT	Geographic Longitude, $^\circ$ E	Observed Count Rate, c/s	Time, UT	Geographic Longitude, $^\circ$ E	Observed Count Rate, c/s
0020	171	34	0000	358	3
0205	147	35	1018	196	2.1
0422	59	43	1238	160	2.1
1100	42	41	2133	34	1
1255	345	38	2316	8	2
1449	318	87			
1602	291	32			
2336	184	40			

note that the  $>1.2$ -Mev electrons behave in the same manner as the  $>280$ -kev electrons. This permits the observation that high-energy electrons in general behave in the same, rather well-defined manner in the outer zone during periods of magnetic quiet.

There is a certain amount of jumpiness in the high-energy electron behavior; to be sure, but in the mean the behavior seems well regulated. It is further illustrated in Table 1, where we show the observed electron intensity at the noon and at the midnight meridian at various times in the day. The representative latitude

shown indicates a relatively stable intensity at both the noon and midnight meridians throughout the day.

Using the mean values of all the data in Figure 2, we have obtained the amount of meridional shift,  $\Delta\lambda = \lambda_D - \lambda_N$ , for both  $E_e \geq 280$  kev and  $E_e \geq 1.2$  Mev, and we show this shift,  $\Delta\lambda$ , as a function of daytime latitude in Figure 3. The data in Figure 3 will be compared, in a later section, with the predictions of various magnetic field models. We point out here, once again, the regularity of the mean values of the matched pass points, indicating

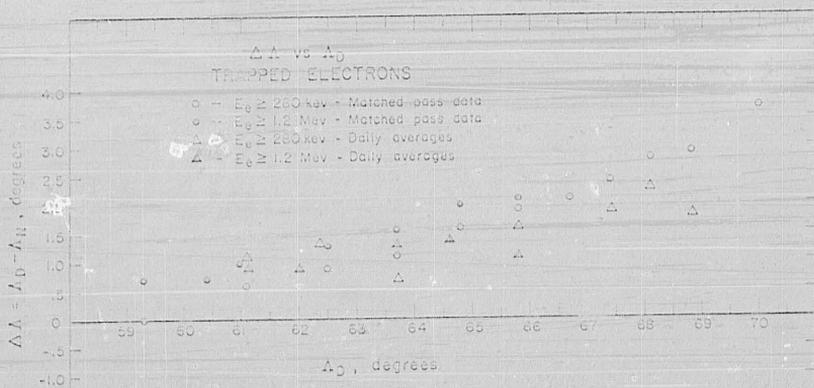


Fig. 3. Plot of the latitude shift,  $\Delta\lambda = \lambda_D - \lambda_N$ , versus nighttime latitude,  $\lambda_D$ . Matched pass data points are obtained from the mean values of the data shown in Figure 2. Daily average data points are also mean values obtained from data similar to those shown in Figure 2. See text for discussion. Bars represent entire spread of values observed during the time period October 2-12, 1962.

a well-defined behavior for the electron population during magnetic quiet.

The two representative bars in Figure 3 indicate the entire range of values seen with the data throughout the time period under study.

2. Daily averages. For each 24-hour interval in this time period we constructed the average latitude profile for both  $E_s \geq 280$  kev and  $E_s \geq 1.2$  Mev for the noon and midnight hemispheres. Using such daily average curves to obtain, on any given day, the daytime and nighttime latitudes,  $A_d$  and  $A_n$ , respectively, corresponding to a constant count rate, yields results that are less affected by uneven pass distributions and decay effects than the curves of Figure 1.

This was done for the 11 days of the time interval under study, and the resulting  $A_d$  and  $A_n$  values were displayed on a plot similar to that shown in Figure 2 for the matched pass data. The resulting plot was very similar to Figure 2, and we show in Figure 3 the mean values of all the data obtained by the method of daily averages.

We note that the daily average data show somewhat more scatter than the matched pass data, as might be expected since the daily average data will be affected by magnetic variations taking place within a 24-hour period whereas the matched pass data are only affected by magnetic variations taking place within  $\sim 50$  minutes. Nevertheless, the daily average data do provide an additional check on the accuracy of the matched pass data and are seen to be consistent with the detailed trend of the dependence of the diurnal shift with latitude.

The data in Figure 3 further indicate that electrons of both  $E_s \geq 280$  kev and  $E_s \geq 1.2$  Mev behave in a similar manner, supporting the previous observation that high-energy electrons in general display the same spatial behavior in the outer zone during periods of magnetic quiet.

#### THEORETICAL CONSIDERATIONS

In this section we present calculations of the diurnal shift in latitude of mirroring particles that should be expected, assuming the conservation of the first two invariants and the particle energy. The first or magnetic moment invariant is given by

$$\mu = p_{\perp}^2/2m\dot{\omega} = p^2/2mB_s \quad (1)$$

in its relativistic form (Northrup, 1965); if energy is conserved, a consequence of the first invariant is that a particle will always mirror at the same value of magnetic field  $B_s$ . The only way the mirror point can be raised or lowered is for the particle to be scattered or for its energy to change, owing to the presence, for example, of electric fields or time-varying magnetic fields.

The second or longitudinal invariant is given by

$$J = \int_M^{M'} p_{\parallel} ds \quad (2)$$

where the line integral is taken along the magnetic line of force between the mirror point  $M$  and its conjugate  $M'$ . Using  $p_{\parallel}^2 = p^2 - p_{\perp}^2$  and (1), this can be rewritten as

$$J = p \int_M^{M'} \left( 1 - \frac{B_s}{B_m} \right)^{1/2} ds \quad (3)$$

assuming that  $p$  is constant over a bounce period. It is convenient then to define an integral invariant  $I$  having the dimensions of a length

$$I \equiv \frac{J}{p} = \int_M^{M'} \left( 1 - \frac{B_s}{B_m} \right)^{1/2} ds \quad (4)$$

which will be conserved as long as the momentum, and thus the energy, is conserved. This integral is independent of the particle energy and depends only on the mirror point and the magnetic field configuration. If particles do not exchange energy as they drift around the earth, their mirror points will always be found on a line of constant  $I$ , meaning, of course, that they are not scattered. If loss rates and production rates are slow compared with one drift period (about 1/2 hour for 280-kev electrons at  $L = 5$ ), we would therefore expect to find approximately equal fluxes of mirroring particles at every point of constant  $B_s$  and  $I$ . The shortest decay times for trapped electrons at these latitudes have been observed to be 1/2 to 1 day, which is more than 10 times as long as the drift times [Williams and Smith, 1965].

Under the above set of assumptions, therefore, the problem of predicting the diurnal shift in latitude of mirroring particles reduces to calculating the integral invariant  $I$  at constant  $B_s$  as a function of latitude, longitude, and local time, and determining the locus of points where  $I$  is constant. In the present instance, we may

eliminate the effect of local field irregularities due to non-dipolar terms, since the contour lines have been expressed as a function of invariant latitude in an equivalent dipole field. Thus, latitude and local time are the important variables.

To calculate  $I$ , we must have a model of the magnetic field. Three such models are used here. The first, given by Mead [1964], is based on the solution to the Chapman-Ferraro problem of a solar wind perpendicularly incident on a dipole field. A surface is formed that separates the earth's field from the infinitely conducting, field-free solar wind. The currents on this surface, or magnetopause, modify the field inside the magnetosphere, the major effect being a general compression of the field lines. The resulting distortion of the magnetic field can most conveniently be described in terms of a spheroidal harmonic expansion, the coefficients determined by making a least-squares fit to the distorted field as calculated at a number of points inside the magnetosphere. The distortion

depends on the strength of the solar wind, and in Mead's model the dependence is brought in through the parameter  $\gamma$ , the distance to the boundary in the solar direction.

The shape of the field lines in the noon-midnight meridional plane is shown in Figure 4 of Mead [1964] for the case  $r_0 = 10$  earth radii. It is seen there that the effect of field line compression is negligible for lines emerging from latitudes less than  $66^\circ$  ( $Z = 1$ ). At higher latitudes the effect becomes significant, and at  $Z = 75^\circ$ , where the dipole line would normally cross the equator at about 15 earth radii, the equatorial crossing distances in the distorted field are 8.7 and 11.2 earth radii on the noon and midnight meridians, respectively. Thus, the surface currents compress the field lines on both the dayside and the nightside, although not as much on the nightside.

The integral invariant as defined by (4) was calculated as a function of latitude on the noon and midnight meridians for particles mirroring at 1100 km (geocentric distance of 1.17 earth

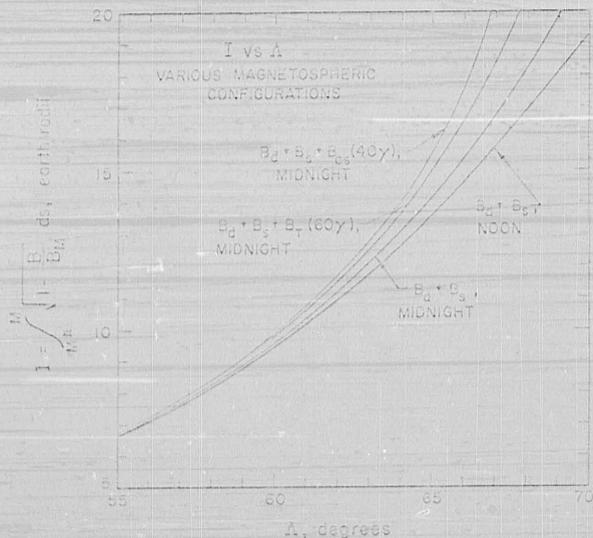


FIG. 4. Plot of the integral invariant,  $I$ , versus field line latitude at 1100 km,  $A$ , for various magnetospheric configurations.  $B_d + B_s$  is the model described by Mead [1964].  $B_T$  ( $60\gamma$ ) is an additional constant field component of magnitude  $60\gamma$ , solar oriented in the northern hemisphere and antisolar oriented in the southern hemisphere.  $B_c$  ( $40\gamma$ ) is a current sheet in the magnetospheric tail yielding a  $40\gamma$  field adjacent to the sheet. See text for discussion.

radii). The results for the dipole field plus surface current field (characterized referred to as  $B_z$  or  $B_1$ ) as given by Mead's model for  $\gamma = 10$  earth radii are shown in Figure 4. The day-night change in latitude for constant  $L$ 's is seen to be about  $1^\circ$  at  $70^\circ$ ; somewhat similar results were obtained by *Malville* [1950], who used an image dipole model for his calculations.

Thus, a simple compression of the magnetosphere by means of surface currents does not predict the observed shifts of several degrees at  $70^\circ$ . However, recent magnetic field measurements by *Ness* [1955] in the tail of the magnetosphere by the Imp 1 satellite has shown that the field configuration in this region is much different from that given by Mead's model. Beyond 10 earth radii, the field in the tail is found to be predominantly in the solar or antisolar direction, instead of perpendicular to the magnetic equator. In addition, a neutral surface separating antisolar directed fields in the southern hemisphere from solar directed fields in the northern hemisphere has been detected over a large area. The presence of such a neutral sheet implies that plasma currents inside the magnetosphere contribute strongly to the magnetic field configuration in the tail region. The presence of such internal plasmas is specifically excluded from the usual Chapman-Ferraro problem, however, suggesting that Mead's model should be modified to take the presence of these plasma currents into consideration.

The simplest way to do this is to vectorially add an additional tail field,  $B_z$ , which is directed away from the sun in the southern hemisphere and toward the sun in the northern hemisphere. Such a field would be produced by an infinite sheet of current in the equatorial plane directed opposite to the earth's orbital velocity vector. The integral invariant on the midnight meridian with an additional  $60\text{-}\gamma$  tail field of this type (denoted by  $B_1 + B_2 + B_3$  [40  $\gamma$ ]) has been calculated and is shown in Figure 4.

If the plasma currents producing the additional field in the tail are strongest in the region past 8 or 10 earth radii, the resulting field due to these currents will not be simply directed away from or toward the sun but will also have a southward component opposing the earth's dipole field, as has been pointed out by *Acford et al.* [1955]. Such a configuration can be

roughly approximated by a truncated semi-infinite current sheet that does not begin until some distance back of the earth. The geometry is shown in Figure 5. The  $x$  axis points away from the sun, and the  $y$  axis points south. The field due to such a current sheet is given by

$$B_x = -2j(y - y_1)$$

$$B_y = 2j \log r_2/r_1$$

where  $j$  is the current per unit length in the sheet in electromagnetic units. The current sheet must have both an inner and an outer cutoff to avoid a logarithmic infinity in the value of  $B_y$ .

The magnetic field configuration in the noon-midnight meridian plane due to the addition of such a current sheet (the total field denoted by  $B_1 + B_2 + B_3$  [40  $\gamma$ ]) has been calculated; it is shown in Figure 6. The current sheet begins at 10 earth radii back of the earth and ends of arbitrarily at 30 earth radii. The current strength is such as to produce a field of  $30\text{-}\gamma$  immediately adjacent to the sheet. The major difference between this configuration and Figure 4 of *Mead* [1961] lies in the direction and strength of the field in the tail region. In the earlier model the field lines were roughly perpendicular to the solar direction in the equatorial region. The same is still true in the present model only to about 7 earth radii, but beyond this point the field lines are open and parallel to the current sheet. The latitude separating the closed lines from the open lines can

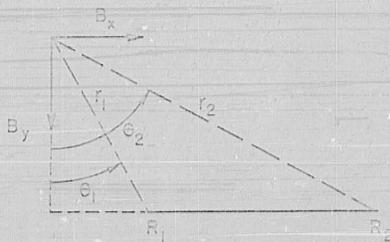


Fig. 5. Diagram showing coordinates used for computation of field due to a truncated semi-infinite current sheet ( $B_3$ ) coincident with the magnetic equatorial plane and extending radially from  $R_1$  to  $R_2$ . It is infinite in length in a direction normal to the paper. The current flow is out of the paper.

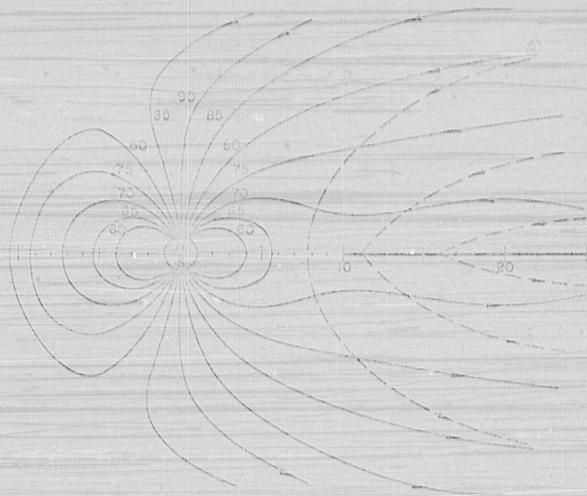


Fig. 6. Solid lines show the field lines in the noon-midnight meridian plane obtained by adding a current sheet in the tail of the model originally discussed by Mead (1964). This configuration was used to obtain the curve labeled  $B_z + B_y + B_x$  ( $40 \gamma$ ) in Figure 4. Dashed lines show field-line continuation of the field due to the current sheet alone. Latitudes shown are those at which field lines intersect the surface of the earth. This configuration fits the experimental observations of trapped electron latitude shifts.

the night side is  $60^\circ$  at the earth's surface, or  $67^\circ$  at an altitude of 1100 km in the auroral zone. Therefore we should not expect to find particles trapped above  $\sim 67^\circ$  on the nightside at 1100 km, and the second invariant is no longer defined above this latitude. Note, however, that the position of the 'mirrored latitude' on the dayside, separating field lines that pass back over the pole into the tail region, is essentially unchanged at about  $82^\circ$  at the earth's surface, well above the auroral zone.

The integral invariant corresponding to this field configuration on the nightside ( $B_z + B_y + B_x$  ( $40 \gamma$ )) was calculated and is shown in Figure 4. The effect of a finite current sheet producing a  $40\gamma$  field is seen to be greater than that of an infinite sheet producing a  $60\gamma$  field. The explanation is the presence of the southward component with the finite current sheet. This component, together with the parallel component, is more effective in extending field lines than the parallel component alone. For high-latitude, low-altitude mirroring particles, the

integral invariant is essentially a measure of the length of the field line, since the integrand is essentially unity except near the mirror points. Thus, any phenomena that tend to stretch out the field lines on the nightside will enhance the day-night latitude shift. Conversely, anything tending to compress the lines further on the dayside, such as an increase in solar wind intensity, will also enhance the day-night difference. A closer boundary plus a reduced current sheet field would produce about the same results. The configuration on the dayside, however, was chosen to match the observed boundary position of about 10 earth radii in the solar direction during quiet periods.

#### DISCUSSION

We present in Figure 7 a comparison of the experimental observations of the latitude shift,  $\Delta\lambda$ , with the computed shift for various magnetic configurations, based on particle drift motions through the magnetosphere under

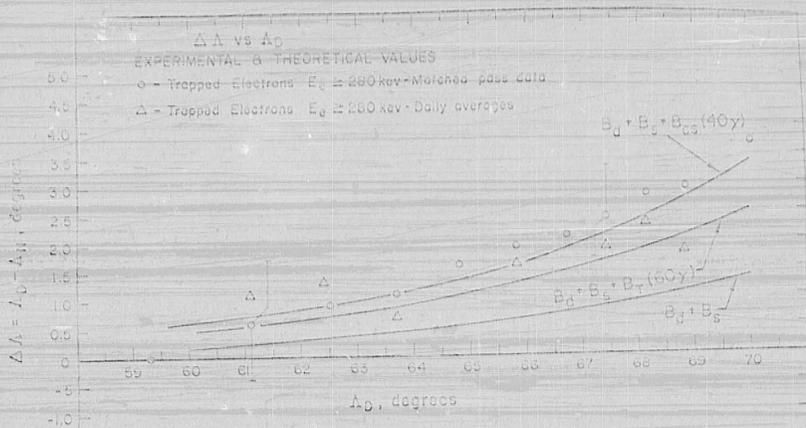


Fig. 7. Comparison of observed latitude shifts with predictions of various magnetic field configurations. All data and calculations are on noon-midnight meridian. The  $\geq 280$ -kev data points are taken from Figure 4, and they are representative of high-energy electrons in general. The curves are obtained directly from Figure 4 for the field configurations shown.

the conservation of the adiabatic invariants. The theoretical curves shown in this figure are obtained directly from the  $I$  versus  $\Lambda$  curves in Figure 4.

Because both electron energies studied,  $E_0 \geq 280$  kev and  $\geq 12$  Mev, display the same diurnal variation, we show only the  $E_0 \geq 280$  kev data in Figure 7 and consider them to be representative of high-energy trapped electrons in general. The bars indicate the entire range of values seen in this time period.

It is clear from Figure 7 that, of the field configurations depicted, the one employing the original model of Mead [1964] plus a current sheet located in the magnetospheric tail,  $B_d + B_s + B_{cs}$  (40  $\gamma$ ), best fits the experimental observations.

A truncated semi-infinite current sheet will obviously lead to inconsistencies when the field configuration away from the noon-midnight meridian is considered. However, all the data are obtained within  $8^\circ$  of the noon-midnight meridian, and such a current sheet should yield results that might appropriately be compared with the data.

The form of the current sheet, extending radially from 10 to 40 earth radii and being of constant magnitude, is to some degree arbit-

rary. A more appropriate distribution, one decreasing in magnitude at large radial distances [Ness, 1965], might be preferable, in general, moving the front edge of the current sheet closer to the earth's surface, or extending the sheet farther away from the earth and simultaneously lowering the current, will give a satisfactory fit to the data. In Table 2 we show two additional current sheet configurations that also fit the observed trapped electron diurnal variations.

We note that, although the field strengths near the current sheet agree with some of the measurements reported by Ness [1965] in the tail region, they are in general somewhat larger than his observations. For example, Ness shows that the field in the tail region decreases to

TABLE 2. Current Sheet Parameters Yielding Fits to Experimental Observations

Front Edge of Current Sheet, earth radii	Rear Edge of Current Sheet, earth radii	Field Strength Adjacent to Sheet, $\gamma$
10	40	40
8	40	33
8	100	23

$\sim 10^\circ$  at 30 earth radii, whereas all our values are somewhat larger than this. (The field due to the dipole plus surface currents is negligible in this region.) There are perhaps two reasons for the disagreement. (1) The effects of a ring current have been neglected and will have to be included when more is known about the characteristics of such a source. Outside the ring current the field lines will be extended, but to a greater extent on the nightside hemisphere, thereby reducing the current sheet intensity below the values we found necessary to match the diurnal shifts. (2) A more realistic current distribution should match the observed variation of  $B$  with distance from the earth [Ness, 1965]. Such a distribution, relatively strong near the earth but weaker in the more distant regions, would probably produce roughly the same effect as the current distributions used above.

Nevertheless, the results of this analysis indicate that the nightside geomagnetic field is an 'open' tail configuration and that the current sheet parameters required to fit the trapped electron data are reasonably compatible with the few direct observations available in the nightside magnetic field.

Noon and midnight high-latitude cutoffs for trapped 40-keV electrons have been reported by O'Brien [1963], McDermid and Barrow [1964], and Frank *et al.* [1964]. All these

measurements show the following general characteristics for the high-latitude boundary of trapping for  $\geq 40$ -keV electrons: (1) the average nighttime high-latitude cutoff at  $\sim 1100$  km is in the range  $71^\circ \lesssim \Lambda_N \lesssim 76^\circ$ , whereas the average midnight boundary at  $\sim 1100$  km is in the range  $67^\circ \lesssim \Lambda_N \lesssim 69^\circ$ . Further, using the intensity contours given in Frank *et al.* [1964], we have constructed a  $\Delta\Lambda$  versus  $\Lambda_N$  plot for  $\geq 40$ -keV electrons in the noon-midnight meridian; we present these results, and for comparison the  $\geq 280$ -keV results, in Figure 8. Note that  $\Lambda_N$  is given for an altitude of 1100 km. Figure 8 clearly shows that  $\geq 40$ -keV trapped electrons undergo significantly larger diurnal shifts than  $\geq 280$ -keV electrons.

The results of Williams and Palmer [1965] indicate that, at an altitude of 1100 km, during times of relative magnetic quiet, the average nighttime and midnight high-latitude trapping boundaries for  $\geq 280$ -keV electrons are  $\sim 68.5^\circ$  and  $\sim 66^\circ$ , respectively. Further, the maximum quiet-time noon and midnight trapping boundaries observed were  $70^\circ$  and  $67^\circ$ , respectively. These observations indicate that both  $\geq 40$ - and  $\geq 280$ -keV electrons have a nightside high-latitude trapping boundary of  $\sim 67^\circ$  at 1100 km. This value is in good agreement with the field configuration shown in Figure 6, which yields a nightside latitude boundary of  $67^\circ$  at 1100 km. This latitude corresponds to the low-

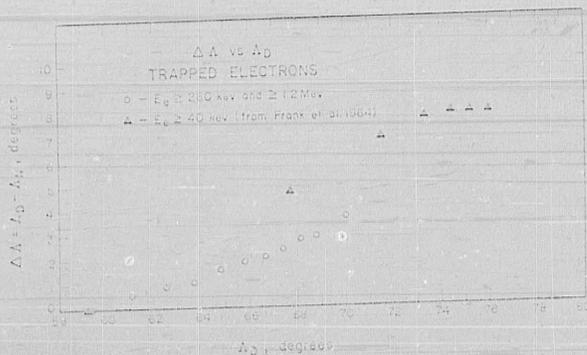


Fig. 8. Comparison of the latitude shifts of  $\geq 40$ - and  $\geq 280$ -keV trapped electrons. The 40-keV data were obtained from the results of Frank *et al.* [1964] and were adjusted to an altitude of 1100 km. The figure shows the significantly larger shifts undergone by the lower-energy trapped electron population.

est latitude field line that displays an 'open' characteristic, i.e., is not connected at the equator.

Thus, the differences in the  $\geq 40$ - and  $\geq 280$ -keV trapped electron spatial characteristics, as shown in Figure 8, seem to be associated with the sunlit hemisphere. It is here that  $\geq 40$ -keV trapped electrons are found at significantly higher latitudes than  $\geq 280$ -keV trapped electrons, in contrast to the nightside situation where the high-latitude boundary is the same for both  $\geq 40$ - and  $\geq 280$ -keV electrons. All this is consistent with the existence of a permanent injection (or acceleration) mechanism on the sunlit part of the magnetosphere. This hypothesis (O'Brien, 1963) is further strengthened by observations of a dayside maximum in the  $\geq 40$ -keV precipitated electron intensities (McDiarmid and Barrows, 1964b; Frank *et al.*, 1964). The relative behavior of the  $\geq 40$ - and  $\geq 280$ -keV electrons imposes a reasonable energy dependence on the injection processes.

Comparison of the  $\geq 40$ - and  $\geq 280$ -keV electron trapping boundary is subject to uncertainties due to the large temporal variations observed in these intensities. However, the results of Williams and Palmer (1965) show that all the  $\geq 40$ -keV data would have to have been obtained from periods of intense magnetic activity to explain the larger shifts observed for the  $\geq 40$ -keV electrons. The  $\geq 40$ -keV observations have, in fact, been taken during periods of low to moderate activity (O'Brien, 1963; McDiarmid and Barrows, 1964a and b; Frank *et al.*, 1964), and so the differences do not seem to be due to differences in magnetic activity.

Another source of uncertainty in the relative  $\geq 40$ - and  $\geq 280$ -keV electron trapping boundary is the effect of a varying dipole orientation in the solar wind. The  $\geq 280$ -keV trapped electron data come from within  $\sim 8^\circ$  of the noon-midnight meridian in October, a time when the dipole axis varies  $\sim \pm 12^\circ$  from the normal to the earth-sun line. The  $\geq 40$ -keV data are presumably obtained from all orientations observed and are not knowingly restricted to any preferred orientation. The agreement among the observations at  $\geq 40$ -keV implies that either the dipole orientation produces only a small effect at most, or that long enough time intervals were sampled so that reproducible averages over dipole orientation were obtained. In

either case, comparisons with the  $\geq 280$ -keV data should be significant.

#### SUMMARY AND CONCLUSIONS

The spatial distribution of high-energy ( $E_e \geq 280$  keV) trapped electrons in the outer zone during periods of magnetic quiet is consistent with the drift of these particles through a distorted magnetosphere under the conservation of the adiabatic invariants. The similarity in the behavior of  $\geq 280$ -keV and  $\geq 1.2$ -MeV trapped electrons allows the above conclusion to extend to high-energy electrons in general.

Detailed observations of the diurnal shift of high-energy trapped electrons ( $E_e \geq 280$  keV and  $\geq 1.2$  MeV) in the noon-midnight meridian were obtained as a function of geomagnetic latitude during magnetic quiet at a time when the earth's magnetic dipole axis varied  $\sim \pm 12^\circ$  from the normal to the earth-sun line. Their using a dayside magnetic field configuration chosen to agree with the measurements of Ness *et al.* (1964), a nightside magnetic field configuration was determined by fitting the measurements of the trapped electron diurnal variations. The resulting magnetic field, shown in Figure 9, is seen to have 'open' configuration due to a current sheet located in the magnetic equatorial plane. This current sheet is a truncated semi-infinite sheet extending radially from 10 to 40 earth radii and gives a field strength of 40  $\gamma$  adjacent to the sheet surface. Field lines due to the sheet alone are also shown in Figure 9. Variations of the current sheet parameters are possible; they are shown in Table 2. This nightside field configuration, as determined by trapped electron behavior at high latitude and low altitude, is quite consistent with the direct magnetic measurements which do exist at  $\geq 10$  earth radii in the nightside hemisphere (Ness, 1965) and agrees closely with the configurations recently suggested by Dessler and Jubin (1965) and Asford, Petschek, and Siscoe (1965).

Therefore, we conclude that the observations of the diurnal variation of high-energy ( $E_e \geq 280$  keV) trapped electrons is consistent with the motion of these electrons in such a distorted magnetosphere under conservation of  $J_\parallel$  and  $E$ .

Using this configuration, we can make the further observation that the average behavior of high-energy electrons ( $E_e \geq 280$  keV) dur-

ing magnetic quiet is well ordered and stable, apart from a steady decay of particles from these low-altitude regions. The observed decay times are in general much longer than the particle drift periods in these regions [Williams and Palmer, 1965] and thus also imply a certain amount of stability to the trapped population.

Finally, we note that at 1100 km both the  $\geq 40$ - and the  $\geq 280$ -kev trapped electrons exhibit the same high-latitude boundary at  $\approx 67^\circ$  at midnight, which agrees well with the high-latitude boundary of closed field lines of  $67^\circ$  in the nightside magnetic field configuration obtained in this study. However, the daytime trapping boundary for  $\geq 40$ -kev electrons extends to significantly higher latitudes than the boundary for  $\geq 280$ -kev electrons. This yields the larger diurnal shifts obtained for the  $\geq 40$ -kev electrons (O'Brien, 1969; McDiarmid and Burrows, 1969a and b; and Frank *et al.*, 1964) and implies a source mechanism operating on the sunlit hemisphere.

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(Manuscript received April 14, 1965.)

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COMPILER OPTIONS - NAME= MAIN,OPT=00,LINFCNT=58,SOURCE,EBCDIC,NOLIST,NODECK,LOAD,MAP,NOEDIT,LD,XREF
ISN 0002   SUBROUTINE MAGTAL(RP,SINTH,COSTH,SINPHI,COSPHI,RO,RI,R2,BCS,
           1 BR,BTHETA,BPHI)
           C   FORTRAN IV PROGRAM TO COMPUTE THE EARTHS DIPOLE FIELD DISTORTED BY
           C   THE SOLAR WIND AND GEOMAGNETIC TAIL (JGR 69, 1181, 1964 AND 70,
           C   3017, 1965), SOLAR WIND IS ASSUMED PERPENDICULAR TO DIPOLE AXIS.
           C   INPUT ARE GEOCENTRIC DISTANCE IN EARTH RADII (RR), GEOMAGNETIC
           C   COLATITUDE(SINTH,COSTH), AND LOCAL TIME MEASURED FROM NOON MERIDI-
           C   AN (SINPHI, COSPHI), SUBSOLAR DISTANCE TO MAGNETICPAUSE (RO), DIS-
           C   TANCE TO FRONT AND BACK EDGE OF TAIL CURRENT SHEET (R1 AND R2),
           C   AND MAGNITUDE OF TAIL FIELD ADJACENT TO SHEET (BCS). THUS SUBSOLAR
           C   POINT IS THETA = 90., PHI = 0. OUTPUT ARE THREE COMPONENTS OF
           C   DISTORTED FIELD, INCLUDING DIPOLE, IN GAMMAS.
ISN 0003   DIMENSION GG(7,7)
ISN 0004   DIMENSION G(7,7),CONST(7,7),P(7,7),DP(7,7),SP(7),CP(7)
ISN 0005   IF(JFIRST = 13) 10,15,10
ISN 0006   10 JFIRST = 13
           C   SET UP INITIAL CONSTANTS THE FIRST TIME AROUND
ISN 0007   DO 5 N=1,7
ISN 0008   DO 5 M=1,7
ISN 0009   5 GG(N,M) = 0.
ISN 0010   NMAX = 7
           C   THE FOLLOWING COEFFICIENTS ARE SCHMIDT-NORMALIZED
ISN 0011   GG(2,1) = -0.25111 E5
ISN 0012   GG(3,2) = -0.12424 E5
ISN 0013   GG(4,1) = -0.00716 E5
ISN 0014   GG(4,3) = -0.02333 E5
ISN 0015   GG(5,2) = -0.02397 E5
ISN 0016   GG(5,4) = -0.00163 E5
ISN 0017   GG(6,1) = 0.00569 E5
ISN 0018   GG(6,3) = -0.01078 E5
ISN 0019   GG(6,5) = -0.00103 E5
ISN 0020   GG(7,2) = 0.00126 E5
ISN 0021   GG(7,4) = -0.00187 E5
ISN 0022   GG(7,6) = -0.00041 E5
ISN 0023   P(1,1) = 1.0
ISN 0024   DP(1,1) = 0.
ISN 0025   SP(1) = 0.
ISN 0026   CP(1) = 1.
ISN 0027   DO 12 N=3,NMAX
ISN 0028   FN = N
ISN 0029   N2 = N - 2
ISN 0030   DO 12 M=1,N2
ISN 0031   FM = M
ISN 0032   12 CONST(N,M) = ((FN-2.)*N**2 - (FM-1.)*M**2) / ((2.*FN-3.)*(2.*FN-5.))
ISN 0033   DIMENSION SHMIDT(7,7)
ISN 0034   SHMIDT(1,1) = 1.0
ISN 0035   DO 820 N=2,7
ISN 0036   FN = N
ISN 0037   SHMIDT(N,1) = SHMIDT(N-1,1)*(FN+FN-3.0)/(FN-1.0)
ISN 0038   FACT = 2.0
ISN 0039   DO 820 M = 2,N
ISN 0040   FM = M
ISN 0041   SHMIDT(N,M) = SHMIDT(N,M-1)*SQRT ((FN-FM+1.0)*FACT/(FN+FM-2.0))
ISN 0042   820 FACT = 1.0
ISN 0043   15 IF(RO-ROOLD) 16,20,16
ISN 0044   16 ROOLD = RO

```

```

ISN 0045     DIMENSION FAC(7)
ISN 0046     FAC(2) = RO**3
ISN 0047     DO 17 N=3,NMAX
ISN 0048     17 FAC(N) = RO * FAC(N-1)
ISN 0049     DO 18 N=2,NMAX
ISN 0050     DO 19 M=1,N
ISN 0051     18 G(N,M) = SHMIDT(N,M) * GG(N,M) / FAC(N)
ISN 0052     20 CONTINUE
C           BEGIN CALCULATION FOR SPECIFIED INPUT
ISN 0053     30 CT = COSTH
ISN 0054     ST = SINTH
ISN 0055     SP(2) = SINPHI
ISN 0056     CP(2) = COSPHI
C           CALCULATE SIN(M*PHI) AND COS(M*PHI)
ISN 0057     DO 41 M=3,NMAX
ISN 0058     SP(M) = SP(2)*CP(M-1) + CP(2)*SP(M-1)
ISN 0059     41 CP(M) = CP(2)*CP(M-1) - SP(2)*SP(M-1)
ISN 0060     R = RR
ISN 0061     A = 1.
ISN 0062     RA = R/A
ISN 0063     ROA = 1.
ISN 0064     BR = 0.
ISN 0065     BTHETA = 0.
ISN 0066     BPHI = 0.
ISN 0067     FN = 1.
C           CALCULATE SPHERICAL HARMONICS FOR CAVITY FIELD
ISN 0068     DO 50 N=2,NMAX
ISN 0069     SUMR = 0.
ISN 0070     SUMT = 0.
ISN 0071     SUMP = 0.
ISN 0072     FM = 0.
C           DEVELOP LEGENDRE FUNCTIONS AND THEIR DERIVATIVES BY RECURSION FORMULAE
ISN 0073     DO 49 M=1,N
ISN 0074     IF(N-M-1) 44,43,42
ISN 0075     42 P(N,M) = CT*P(N-1,M) - CONST(N,M)*P(N-2,M)
ISN 0076     DP(N,M) = CT*DP(N-1,M) - ST*P(N-1,M) - CONST(N,M)*DP(N-2,M)
ISN 0077     GO TO 45
ISN 0078     43 P(N,M) = CT * P(N-1,M)
ISN 0079     DP(N,M) = CT*DP(N-1,M) - ST*P(N-1,M)
ISN 0080     GO TO 45
ISN 0081     44 P(N,N) = ST * P(N-1,N-1)
ISN 0082     DP(N,N) = ST*DP(N-1,N-1) + CT*P(N-1,N-1)
ISN 0083     45 CONTINUE
ISN 0084     TS = G(N,M) * CP(M)
ISN 0085     SUMR = SUMR + P(N,M)*TS
ISN 0086     SUMT = SUMT + DP(N,M)*TS
ISN 0087     SUMP = SUMP + FM*P(N,M)*G(N,M)*SP(M)
ISN 0088     FM = FM + 1.
ISN 0089     49 CONTINUE
ISN 0090     BR = BR - ROA*FN*SUMR
ISN 0091     BTHETA = BTHETA - ROA*SUMT
ISN 0092     BPHI = BPHI + ROA*SUMP
ISN 0093     ROA = ROA * RA
ISN 0094     FN = FN + 1.
ISN 0095     50 CONTINUE
ISN 0096     BPHI = BPHI / ST

```

```
C      ADD DIPOLE FIELD TO CAVITY FIELD
ISN 0097      R3 = R**3
ISN 0098      BR = BR - 52000. * COSTH / R3
ISN 0099      BTHETA = BTHETA - 31000. * SINTH / R3
C      CALCULATE TAIL FIELD
ISN 0100      IF(BCS,EO,0.) RETURN
ISN 0102      RCT = R * CT
ISN 0103      RCT2 = RCT**2
ISN 0104      RSC = R * ST * CP(2)
ISN 0105      TOP = R2 + RSC
ISN 0106      BOT = R1 + RSC
ISN 0107      BX = -BCS * (ATAN(TOP/RCT) - ATAN(BOT/RCT)) / 3.14159265
ISN 0108      BPHI = BPHI + BX * SP(2)
ISN 0109      BRHO = -BX * CP(2)
ISN 0110      BY = BCS * ALOG((RCT2+TOP**2)/(RCT2+BOT**2)) / 6.28318531
ISN 0111      BR = BR + BRHO*ST - BY*CT
ISN 0112      BTHETA = BTHETA + BRHO*CT + BY*ST
ISN 0113      GO RETURN
ISN 0114      END
```



SYMBOL	INTERNAL STATEMENT NUMBERS
MAGTAL	0002
SHMIDY	0033 0034 0037 0037 0041 0041 0051
SINPHI	0002 0055

LABEL	DEFINED	REFERENCES
5	0009	0007 0008
10	0006	0005 0005
12	0032	0027 0030
15	0043	0005
16	0044	0043 0043
17	0048	0047
18	0051	0049 0050
20	0052	0043
30	0053	
41	0059	0057
42	0075	0074
43	0078	0074
44	0081	0074
45	0083	0077 0080
49	0089	0073
50	0095	0068
50	0113	
B20	0042	0035 0039



LABEL ADDR

10 00076A  
15 000P22  
20 000C42  
43 000EEC  
50 0011C0

LABEL ADDR

5 000782  
16 000B36  
30 000C42 NR  
44 000FAA  
60 001384 NR

LABEL ADDR

12 0005E4  
17 000F50  
41 000CB6  
45 001060

LABEL ADDR

820 000AEE  
18 000B9A  
42 000D92  
49 00115A

\*OPTIONS IN EFFECT\*

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\*OPTIONS IN EFFECT\*

SOURCE,EBCDIC,NOLIST,NOPECK,LOAD,MAP,NOEDIT,LD,XREF

\*STATISTICS\*

SOURCE STATEMENTS = 113 ,PROGRAM SIZE = 5174

\*STATISTICS\* NO DIAGNOSTICS GENERATED

\*\*\*\*\* END OF COMPILATION \*\*\*\*\*

IEF2851 SYS71230, T160946, RV000, YZ2RMCD1, ORJMOD PASSED  
 IEF2851 VOL SER NOS= K3SCR2.  
 IEF2851 SYS71230, T160946, SV000, YZ2RMCD1, R0000391 SYSCUT  
 IEF2851 VOL SER NOS= K3SCR5.  
 IEF2851 SYS71230, T160946, SV000, YZ2RMCD1, R0000392 DELETED  
 IEF2851 VOL SER NOS= K3SCR4.  
 IEF2851 SYS71230, T160946, RV000, YZ2RMCD1, R0000393 DELETED  
 IEF2851 VOL SER NOS= K3SCR2.  
 IEF2851 SYS71230, T160946, RV000, YZ2RMCD1, R0000394 DELETED  
 IEF2851 VOL SER NOS= K3SCR2.  
 IEF2851 SYS71230, T160946, SV000, YZ2RMCD1, R0000395 DELETED  
 IEF2851 VOL SER NOS= K3SCR5.  
 IEF2851 SYS71230, T160946, RV000, YZ2RMCD1, S0000396 SYSIN  
 IEF2851 VOL SER NOS= K3SCR3.  
 IEF2851 SYS71230, T160946, RV000, YZ2RMCD1, S0000396 DELETED  
 IEF2851 VOL SER NOS= K3SCR3.

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 IEF3741 STEP /SOURCE / STOP 71230,1753 CPU 00MIN 02,45SEC MAIN 248K LCS OK  
 - STEP 01 - RETURN CODE = 0000

STEP TIME = .11 MINS=(CPU= .04, IO= .07)  
 .00, CELL= .00, OTHR= .28  
 IO IN SECS, DISK= 4.26, DRUM= .11, TAPE=

IEF2851 SYS71230, T160946, RV000, YZ2RMCD1, ORJMOD DELETED  
 IEF2851 VOL SER NOS= K3SCR2.  
 IEF3751 JOB /YZ2RMCD1/ START 71230,1737  
 IEF3761 JOB /YZ2RMCD1/ STOP 71230,1753 CPU 00MIN 02,45SEC  
 - SYSTEM=MVT-12 (12-07-69) K3  
 - JOB 0323-

TOTAL TIME = .11 MINS=(CPU= .04, IO= .07)  
 .00, CELL= .00, OTHR= .28  
 IO IN SECS, DISK= 4.26, DRUM= .11, TAPE=

TIME=17,53,52.55 DATE=08-18-71

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//STEP1 EXEC FORTRANH
XXDEFAULT PROC FORTRAN=IEKAA00,NBLK=40 * FORTRANH * 19 NOV 71 * 00000010
XXSOURCE EXEC PGM=&FORTRAN,REGION=320K,PARM='OPT=1' 00000020
IEF653I SUBSTITUTION JCL - PGM=IEKAA00,REGION=320K,PARM='OPT=1'
XXSTEPLIB DD DSN=SYS1.FORTH,DISP=SHR 00000030
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XX SPACE=(3200,(SNBLK,40),,,ROUND),DCB=(RECFM=FB,LRECL=80,BLKSIZE=3200) 00000050
IEF653I SUBSTITUTION JCL - SPACE=(3200,(40,40),,,ROUND),DCB=(RECFM=FB,LRECL=80,BLKSIZE=3200)
XXSYSPRINT DD SYSOUT=A,UNIT=(2314,SEP=SYSLIN), 00000060
XX DCB=(RECFM=VBA,LRECL=137,BLKSIZE=7265) 00000070
XXSYSPUNCH DD SYSOUT=B,DCB=(RECFM=FB,LRECL=80,BLKSIZE=3200) 00000080
XXSYSUT1 DD UNIT=(2314,SEP=(SYSLIN,SYSPRINT)),SPACE=(CYL,(1,1)) 00000090
XXSYSUT2 DD UNIT=(2314,SEP=(SYSLIN,SYSPRINT,SYSUT1)),SPACE=(CYL,(1,1)) 00000100
//SOURCE.SYSIN DD *
//
IEF236I ALLOC. FOR YZJRJRWP SOURCE STEP1
IEF237I 100 ALLOCATED TO STEPLIB
IEF237I 217 ALLOCATED TO SYSLIN
IEF237I 217 ALLOCATED TO SYSPRINT
IEF237I 213 ALLOCATED TO SYSPUNCH
IEF237I 237 ALLOCATED TO SYSUT1
IEF237I 216 ALLOCATED TO SYSUT2
IEF237I 213 ALLOCATED TO SYSIN

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COMPILER OPTIONS - NAME= MAIN,OPT=01,LIN CNT=58,SOURCE,EBCDIC,NOLIST,NODECK,LOAD,MAP,NODEIT,LD,NEXREF
ISN 0002      SUBROUTINE MAGTAL(RR,SINTH,COSTH,SINPHI,COSPHI,RO,R1,R2,BCS,
              1 BR,BTHETA,BPHI)
              C
              C   FORTRAN IV PROGRAM TO COMPUTE THE EARTH'S DIPOLE FIELD DISTORTED BY
              C   THE SOLAR WIND AND GEOMAGNETIC TAIL (JGR 69, 1181, 1964 AND 70,
              C   3017, 1965). SOLAR WIND IS ASSUMED PERPENDICULAR TO DIPOLE AXIS.
              C   INPUT ARE GEOCENTRIC DISTANCE IN EARTH RADII (RR), GEOMAGNETIC
              C   COLATITUDE (SINTH,COSTH), AND LOCAL TIME MEASURED FROM NOON MERIDI-
              C   AN (SINPHI, COSPHI), SUBSOLAR DISTANCE TO MAGNETOPAUSE (RO), DIS-
              C   TANCE TO FRONT AND BACK EDGE OF TAIL CURRENT SHEET (R1 AND R2),
              C   AND MAGNITUDE OF TAIL FIELD ADJACENT TO SHEET (BCS). THUS SUBSOLAR
              C   POINT IS THETA = 90, PHI = 0. OUTPUT ARE THREE COMPONENTS OF
              C   DISTORTED FIELD, INCLUDING DIPOLE, IN GAMMAS.
              C   DIMENSION GG(7,7)
              C   DIMENSION G(7,7),CONST(7,7),P(7,7),DP(7,7),SP(7),CP(7)
              C   IF(JFIRST - 13) 10,15,10
              C   10 JFIRST = 13
              C   SET UP INITIAL CONSTANTS THE FIRST TIME AROUND
              C   DO 5 N=1,7
              C   DO 5 M=1,7
              C   5 GG(N,M) = 0.
              C   NMAX = 7
              C   THE FOLLOWING COEFFICIENTS ARE SCHMIDT-NORMALIZED
              C   GG(2,1) = -0.25111 E5
              C   GG(3,2) = -0.12424 E5
              C   GG(4,1) = -0.00716 E5
              C   GG(4,3) = -0.02333 E5
              C   GG(5,2) = -0.02397 E5
              C   GG(5,4) = -0.00163 E5
              C   GG(5,1) = 0.00569 E5
              C   GG(6,3) = -0.01078 E5
              C   GG(6,5) = -0.00103 E5
              C   GG(7,2) = 0.00126 E5
              C   GG(7,4) = -0.00187 E5
              C   GG(7,6) = -0.00041 E5
              C   P(1,1) = 1.0
              C   DP(1,1) = 0.
              C   SP(1) = 0.
              C   CP(1) = 1.
              C   DO 12 N=3,NMAX
              C   FN = N
              C   N2 = N - 2
              C   DO 12 M=1,N2
              C   FM = M
              C   12 CONST(N,M) = ((FN-2.)**2 - (FM-1.)**2) / ((2.*FN-3.)*(2.*FN-5.))
              C   DIMENSION SHMIDT(7,7)
              C   SHMIDT(1,1) = 1.0
              C   DO 820 N=2,7
              C   FN = N
              C   SHMIDT(N,1) = SHMIDT(N-1,1)*(FN+FN-3.0)/(FN+1.0)
              C   FACT = 2.0
              C   DO 820 M = 2,N
              C   FM = M
              C   SHMIDT(N,M) = SHMIDT(N,M-1)*SQRT ((FN+FM+1.0)*FACT/(FN+FM-2.0))
              C   820 FACT = 1.0
              C   15 IF(RO*ROOLD) 16,20,16
              C   16 ROOLD = RO

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ISN 0045      DIMENSION FAC(7)
ISN 0046      FAC(2) = RO**3
ISN 0047      DO 17 N=3,NMAX
ISN 0048      17 FAC(N) = RO * FAC(N-1)
ISN 0049      DO 18 N=2,NMAX
ISN 0050      DO 18 M=1,N
ISN 0051      18 G(N,M) = SHMIDT(N,M) * GG(N,M) / FAC(N)
ISN 0052      20 CONTINUE

C          BEGIN CALCULATION FOR SPECIFIED INPUT
ISN 0053      30 CT = COSTH
ISN 0054      ST = SINTH
ISN 0055      SP(2) = SINPHI
ISN 0056      CP(2) = COSEPHI
C          CALCULATE SIN(M*PHI) AND COS(M*PHI)
ISN 0057      DO 41 M=3,NMAX
ISN 0058      SP(M) = SP(2)*CP(M-1) + CP(2)*SP(M-1)
ISN 0059      41 CP(M) = CP(2)*CP(M-1) - SP(2)*SP(M-1)
ISN 0060      R = RR
ISN 0061      A = 1.
ISN 0062      RA = R/A
ISN 0063      RQA = 1.
ISN 0064      BR = 0.
ISN 0065      BTHE TA = 0.
ISN 0066      BPHI = 0.
ISN 0067      FN = 1.
C          CALCULATE SPHERICAL HARMONICS FOR CAVITY FIELD
ISN 0068      DO 50 N=2,NMAX
ISN 0069      SUMR = 0.
ISN 0070      SUMT = 0.
ISN 0071      SUMP = 0.
ISN 0072      FM = 0.
C          DEVELOP LEGENDRE FUNCTIONS AND THEIR DERIVATIVES BY RECURSION FORMULAE
ISN 0073      DO 49 M=1,N
ISN 0074      IF(N-M-1) 44,43,42
ISN 0075      42 P(N,M) = CT*P(N-1,M) - CONST(N,M)*P(N-2,M)
ISN 0076      DP(N,M) = CT*DP(N-1,M) - ST*P(N-1,M) - CONST(N,M)*DP(N-2,M)
ISN 0077      GO TO 45
ISN 0078      43 P(N,M) = CT * P(N-1,M)
ISN 0079      DP(N,M) = CT*DP(N-1,M) - ST*P(N-1,M)
ISN 0080      GO TO 45
ISN 0081      44 P(N,N) = ST * P(N-1,N-1)
ISN 0082      DP(N,N) = ST*DP(N-1,N-1) + CT*P(N-1,N-1)
ISN 0083      45 CONTINUE
ISN 0084      TS = G(N,M) * CP(M)
ISN 0085      SUMP = SUMP + P(N,M)*TS
ISN 0086      SUMT = SUMT + DP(N,M)*TS
ISN 0087      SUMP = SUMP + FN*P(N,M)*G(N,M)*SP(M)
ISN 0088      FM = FM + 1.
ISN 0089      49 CONTINUE
ISN 0090      BR = BR - RQA*FN*SUMP
ISN 0091      BTHE TA = BTHE TA - RQA*SUMT
ISN 0092      BPHI = BPHI + RQA*SUMP
ISN 0093      RQA = RQA * RA
ISN 0094      FN = FN + 1.
ISN 0095      50 CONTINUE
ISN 0096      BPHI = BPHI / ST

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ISN 0097 C ADD DIPOLE FIELD TO CAVITY FIELD
ISN 0098 R3 = R**3
ISN 0099 BR = BR - 62000. * COSTH / R3
          BTHETA = BTHETA - 31000. * SINTH / R3
ISN 0100 C CALCULATE TAIL FIELD
ISN 0101 IF (BCS.EQ.0.) RETURN
ISN 0102 RCT = R * C1
ISN 0103 RCT2 = RCT**2
ISN 0104 RSC = R * ST * CP(2)
ISN 0105 TOP = R2 + RSC
ISN 0106 BOT = R1 + RSC
ISN 0107 BX = -BCS * (ATAN(TOP/RCT) - ATAN(BOT/RCT)) / 3.14159265
ISN 0108 BPHT = BPHT + BX * SP(2)
ISN 0109 BRHC = -BX * CP(2)
ISN 0110 BY = BCS * ALG((RCT2+TOP**2)/(RCT2+BOT**2)) / 6.28318531
ISN 0111 BR = BR + BRHC*ST - BY*CT
ISN 0112 BTHETA = BTHETA + BRHC*CT + BY*ST
ISN 0113 60 RETURN
ISN 0114 END
```



LABEL	ADDR
10	0006F0
15	0009AF
20	000A7E
43	000C42
50	000E36

LABEL	ADDR
5	0005F0
16	0009BE
30	000A7E NR
44	000CB8
60	000FB2 NR

LABEL	ADDR
12	00082A
17	0009DC
41	000AD4
45	000D2A

LABEL	ADDR
820	006984
18	000A12
42	000B78
49	000DD4

\*OPTIONS IN EFFECT\* NAME= MAIN,OPT=01,LINECNT=58

\*OPTIONS IN EFFECT\* SOURCE,FBCDIC,NOLIST,NODE CK,LOAD,MAP,NOEDIT,LD,NOXREF

\*STATISTICS\* SOURCE STATEMENTS = 113 ,PROGRAM SIZE = 4194

\*STATISTICS\* NO DIAGNOSTICS GENERATED

\*\*\*\*\* END OF COMPILATION \*\*\*\*\*

IFF285I SYS1.FOR TH KFPT  
 IFF285I VOL SER NOS= M2DRM1.  
 IFF285I SYS71361.T191747.RV000.YZJRJRWP.CBJMOD PASSED  
 IFF285I VOL SER NOS= M2SCR5.  
 IFF285I SYS71361.T191747.SV000.YZJRJRWP.R0000055 SYSCUT  
 IFF285I VOL SER NOS= M2SCR1.  
 IFF285I SYS71361.T191747.SV000.YZJRJRWP.R0000056 DELETED  
 IFF285I VOL SER NOS= M2SCR5.  
 IFF285I SYS71361.T191747.RV000.YZJRJRWP.R0000057 DELETED  
 IFF285I VOL SER NOS= M2SCR6.  
 IFF285I SYS71361.T191747.RV000.YZJRJRWP.R0000058 DELETED  
 IFF285I VOL SER NOS= M2SCR4.  
 IFF285I SYS71361.T191747.RV000.YZJRJRWP.S0000059 SYSIN  
 IFF285I VOL SER NOS= M2SCR5.  
 IFF285I SYS71361.T191747.RV000.YZJRJRWP.S0000059 DELETED  
 IFF285I VOL SER NOS= M2SCR5.

IFF373I STEP /SOURCE / START 71361.2015  
 IFF374I STEP /SOURCE / STOP 71361.2016 CPU 00MIN 01.10SEC MAIN 298K LCS OK  
 - STEP 01 - RETURN CODE = 0000 STEP TIME = .04 MINS=(CPU= .01,I/O= .03)  
 IO IN SECS. DISK= 2.24,DRUM= .14,TAPE= .00,CELL= .00,OTHR= .32

IFF285I SYS71361.T191747.RV000.YZJRJRWP.CBJMOD DELETED  
 IFF285I VOL SER NOS= M2SCR5.

IFF375I JOB /YZJRJRWP/ START 71361.2015  
 IFF376I JOB /YZJRJRWP/ STOP 71361.2016 CPU 00MIN 01.10SEC TIME=20.16.14.74 DATE=12-27-71  
 - SYSTEM=MVT-12 (12-07-69) M2 TOTAL TIME = .04 MINS=(CPU= .01,I/O= .03)  
 - JOB 0627- IO IN SECS. DISK= 2.24,DRUM= .14,TAPE= .00,CELL= .00,OTHR= .32